

Claims

1. Method for designing a technical system which is characterized by parameters, including state variables and  
5 diagnostic variables which depend on the state variables:
  - in which the technical system is specified by a system of equations, with the state variables being the solutions of the system of equations;  
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  - in which a measurement park, incorporating first measured variables, is analyzed, whereby the first measured variables are measured in the technical system with a prescribed accuracy, and depend on the state variables;  
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  - in which second measured variables, which depend on the state variables, can be measured in the technical system with a predetermined accuracy;
  - 20 - in which first sensitivity variables are determined for the first measured variables and/or second sensitivity variables for the second measured variables;
  - in which, to determine the first sensitivity variables, a  
25 determination is made of the magnitude of the influence which a change in the accuracy of measurement of the first measured variables has on at least one selected parameter, and to determine the second sensitivity variables, a determination is made of the magnitude of the influence  
30 which the measurement of the second measured variables has on at least one selected parameter;
  - in which the measurement park is changed, depending on the

first and/or second sensitivity variables, in such a way that the accuracy of one or more of the first measured variables is changed and/or one or more of the first measured variables is taken out of the measurement park and/or one or more of the second measured variables is added into the measurement park;

- in which the amended measurement park is used in designing the technical system.

2. Method in accordance with claim 1, whereby the accuracy of a first measured variable is increased if the first sensitivity variable for this measured variable lies within a predefined value range and/or a first measured variable is taken out of the measurement park if the first sensitivity variable for this measured variable lies within a predefined value range and/or a second measured variable is added into the measurement park if the second sensitivity variable for this measured variable lies within a predefined value range.

3. Method in accordance with claim 1 or 2, whereby the technical system is described by a system of equations  $H(x) = (H_1(x), \dots, H_m(x)) = 0$ , where  $x = (x_1, \dots, x_n)$  is a vector in which the components are the state variables  $x_i$ .

4. Method in accordance with claim 3, in which the following matrices are calculated:

- a matrix  $N$ , which spans the null space of the Jacobian matrix of  $H$ ,
- a matrix  $W$ , such that  $W^T \cdot W$  is the inverse of the covariance matrix of the first measured variables  $y_i = b_i(x)$ , where the entries in the covariance matrix are the covariances  $\sigma_{ij}^2 = E((y_i - E(y_i))(y_j - E(y_j)))$ , where

$E(y)$  is the expected value of  $y$ ;

- a matrix  $M$  which is the pseudoinverse matrix of  $A=W \cdot Db \cdot N$ , where  $Db$  is the Jacobian matrix of the first measured variables  $y_i=b_i(x)$ .

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5. Method in accordance with claim 4, in which

- at least one of the selected parameters is a selected state variable which can be determined via the first measured variables;
- one or more of the first sensitivity variables  $\Phi_{y_j x_1}$  represents in each case the ratio of the change in accuracy  $\Delta \sigma_{11}^2/x_1 = \Delta E((x_1 - E(x_1))^2)/x_1$  of the selected state variable  $x_1$  to the change in accuracy  $\Delta \sigma_{jj}^2/y_j = \Delta E((y_j - E(y_j))^2)/y_j$  of a first measured variable  $y_j$ ;
- the first sensitivity variables are determined from the following formula:

$$\Phi_{y_j x_1} = \frac{\sigma_{jj}^2}{\sigma_{11}^2} \cdot r_{1j}^2$$

20 where  $r_{1j}$  is the element in the 1<sup>th</sup> line and the  $j^{\text{th}}$  column of the matrix  $N \cdot M \cdot W$ .

6. Method in accordance with claim 4 or 5, in which

- at least one of the selected parameters is a selected diagnostic variable which can be determined via the first measured variables;
- a matrix  $Dd$  is determined, this being the Jacobian matrix of the diagnostic variables  $d_i=d_i(x)$ ;
- one or more of the first sensitivity variables  $\Phi_{y_j d_n}$  represents in each case the ratio of the change in accuracy  $\Delta \sigma_{nn}^2/d_n = \Delta E((d_n - E(d_n))^2)/d_n$  of the selected diagnostic variable  $d_n$  to the change in accuracy  $\Delta \sigma_{jj}^2/y_j = \Delta E((y_j - E(y_j))^2)/y_j$  of a first measured variable  $y_j$ ;

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- the first sensitivity variables are determined by the following formula:

$$\Phi = \frac{\sigma_{jj}^2}{y_j d_n \sigma_{nn}^2} \cdot s_{nj}^2$$

where  $s_{nj}$  is the element in the  $n^{\text{th}}$  line and the  $j^{\text{th}}$  column of  $Dd \cdot N \cdot M \cdot W$ .

7. Method in accordance with one of the claims 4 to 6, in which

- at least one of the selected parameters is a selected state variable which can be determined via the first measured variables;
- one or more of the second sensitivity variables represents, in each case, the variance  $\sigma_{k \rightarrow x1}^2$  of the selected state variable  $x_1$  when a second measured variable, the value of which is a state variable  $x_k$  with the variance  $\sigma_k$ , is being added to the measurement park;
- the second sensitivity variables are determined by the following formula:

$$\sigma_{k \rightarrow x1}^2 = m_1^T \cdot m_1 - \frac{(m_k^T \cdot m_1)^2}{\sigma_k^2 + m_k^T \cdot m_k}$$

where  $m_i$  is the  $i^{\text{th}}$  column of the matrix  $M^T \cdot N$ .

8. Method in accordance with one of the claims 4 to 7, in which

- at least one of the selected parameters is a selected diagnostic variable which can be determined via the first measured variables;
- a matrix  $Dd$ , which is the Jacobian matrix of the diagnostic variables  $d_i = d_i(x)$ , is determined;
- one or more of the second sensitivity variables

represents, in each case, the variance  $\sigma_{k \rightarrow d_n}^2$  of the selected diagnostic variable  $d_n$  when a second measured variable, the value of which is a state variable  $x_k$  which has a variance  $\sigma_k$ , is being added to the measurement park;

- 5 - the second sensitivity variables are determined by the following formula:

$$\sigma_{k \rightarrow d_n}^2 = q_n^T \cdot q_n - \frac{(m_k^T \cdot q_n)^2}{\sigma_k^2 + m_k^T \cdot m_k}$$

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where  $m_i$  is the  $i^{\text{th}}$  column of the matrix  $M^T \cdot N^T$ , and  $q_n$  is the  $n^{\text{th}}$  column of the matrix and  $M^T \cdot N^T \cdot D d^T$ .

9. Method in accordance with one of the claims 4 to 8, in which

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- at least one of the selected parameters is a selected state variable which cannot be determined via the first measured variables;
- a matrix  $P$ , which is the orthogonal projection onto the null space of  $A$ , is determined;
- a second measured variable is determined, the value of which is a state variable  $x_k$ , and which is to be added into the measurement park so that the selected state variable can be uniquely determined;
- one of the second sensitivity variables represents the variance  $\sigma_{k \rightarrow x_1}^2$  of the selected state variable when the second measured variable  $x_k$  which has been determined, and which has the variance  $\sigma_k$ , is being added to the measurement park;
- the second sensitivity variable is determined by the following formula:

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$$\|p\|^2 \quad \| \quad \|p\| \quad \|^2$$

$$\sigma_{k \rightarrow x1}^2 = \sigma_k^2 \cdot \frac{\|p\|^2}{\|p_k\|^2} + \frac{\|m_1 - p_k\|^2}{\|p_k\|^2},$$

with  $p = Pn_1$ , where  $n_1$  is the 1<sup>th</sup> column of the matrix  $N^T$ ,  
 5 and  $m_i$  is the  $i^{\text{th}}$  column of the matrix  $M^T \cdot N^T$  and  $p_k$  is the  
 $k^{\text{th}}$  column of the matrix  $P \cdot N^T$ .

10. Method in accordance with one of the claims 4 to 9, in which

- 10 - at least one of the selected parameters is a selected  
diagnostic variable which cannot be determined via the  
first measured variables;
- a matrix  $D_d$ , which is the Jacobian matrix of the  
diagnostic variables  $d_i = d_i(x)$ , is determined;
- 15 - a matrix  $P$ , which is the orthogonal projection onto the  
null space of  $A$ , is determined;
- a second measured variable is determined, the value of  
which is a state variable  $x_k$ , and which is to be added  
into the measurement park so that the selected state  
20 variable can be uniquely determined;
- one of the second sensitivity variables represents the  
variance  $\sigma_{k \rightarrow d_n}^2$  of the selected diagnostic variable  $d_n$  when  
the second measured variable  $x_k$  which has been determined,  
and which has the variance  $\sigma_k$ , is being added into the  
25 measurement park;
- the second sensitivity variable is determined by the  
following formula:

$$\sigma_{k \rightarrow d_n}^2 = \sigma_k^2 \cdot \frac{\|p\|^2}{\|p_k\|^2} + \frac{\|M^T \cdot c_n - p_k\|^2}{\|p_k\|^2},$$

with  $p = Pc_n$ , where  $c_n$  is the  $n^{\text{th}}$  column of the matrix

$N^T \cdot Dd^T$ ,  $m_k$  is the  $k^{\text{th}}$  column of the matrix  $M^T \cdot N^T$  and  $p_k$  is the  $k^{\text{th}}$  column of the matrix  $P \cdot N^T$ .

5 11. Method in accordance with claim 9 or 10, by which the matrix  $P \cdot N^T$  is searched for the column such that  $p$  is a linear function of this column, where the index  $k$  of this column specifies that the second measurement value  $x_k$  is to be added into the measurement park so that the selected parameter can be uniquely determined.

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12. Method in accordance with one of the claims 7 to 11, in which the standard deviation  $\sigma_k$  of the second measured variable is 1% of the value of the second measured variable.

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13. Device for analyzing a technical system which is equipped in such a way that a method in accordance with one of the preceding claims can be performed.

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14. Computer program produce which has a storage medium on which is stored a computer program which can be executed on a computer and with which the method in accordance with one of the claims 1 to 12 can be performed.